

On optimality of MIA for unknown leakage models and related new practical results

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On the Optimality of Mutual Information Analysis

Authors





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Motivation & State-of-the Art

- As the threat of side-channel attacks is well known. countermeasures are used for protection
- For example: Weakening the link between the measured leakage \mathbf{X} and the sensitive variable \mathbf{Y}

Take home message!



- What is the optimal generic distinguisher?
- By applying the maximum likelihood principle, we derive the optimal generic distinguisher

- Generic distinguisher cope with this scenario
 - Mutual Information Analysis (MIA) [1]
 - Kolmogorov-Smirnov distance (KSA) [2]
 - [3],...

When the leakage has been quantified and probabilities are estimated from histograms, the optimal distinguisher's expression turns out to coincide with the mutual information analysis

[1] Benedikt Gierlichs, Lejla Batina, Pim Tuyls, and Bart Preneel. Mutual information analysis. In CHES, 10th International Workshop, volume 5154 of Lecture Notes in Computer Science, pages 426–442. Springer, August 10-13 2008. Washington, D.C., USA.

[2] Nicolas Veyrat-Charvillon and Fran cois-Xavier Standaert. Mutual Information Analysis: How, When and Why? In CHES, volume 5747 of LNCS, pages 429-443.

Springer, September 6-9 2009. Lausanne, Switzerland.

[3] N. Veyrat-Charvillon and F.-X. Standaert. Generic side-channel distinguishers: Improvements and limitations. In P. Rogaway, editor, CRYPTO, volume 6841 of Lecture Notes in Computer Science, pages 354–372. Springer, 2011.

[4] Julien Doget, Emmanuel Prouff, Matthieu Rivain, François-Xavier Standaert: Univariate side channel attacks and leakage modeling. J. Cryptographic Engineering 1(2): 123-144 (2011)

Universal Maximum Likelihood Equivalent to MIA

Notations & Assumptions

- Values are quantized (discrete leakage) $\hat{\mathbb{P}}(x|y) = \frac{\sum_{i=1}^{m} \mathbb{1}_{x_i=x, y_i=y}}{\sum_{i=1}^{m} \mathbb{1}_{y_i=y}} = \frac{\hat{\mathbb{P}}(x, y)}{\hat{\mathbb{P}}(y)}$
- From the Maximum Likelihood it is known that maximizing the success rate amounts to select the key guess k that maximizes

 $\mathbb{P}(\mathbf{x}|\mathbf{y})$



Empirical Mutual Information

$$\hat{I}(\mathbf{x}, \mathbf{y}) = \sum_{x \in \mathcal{X}, y \in \mathcal{Y}} \hat{\mathbb{P}}(x, y) \log_2 \frac{\hat{\mathbb{P}}(x, y)}{\hat{\mathbb{P}}(x)\hat{\mathbb{P}}(y)}$$

In practice if no profiling is possible the conditional distribution is unknown Therefore, we need a *universal* version (computed from the available data) without prior information)

$$\hat{k} = \arg\max_{k} \hat{\mathbb{P}}(\mathbf{x}|\mathbf{y}) = \arg\max_{k} \prod_{i=1}^{m} \hat{\mathbb{P}}(x_i|y_i)$$

Universal Maximum Likelihood is equivalent to mutual information analysis

$$\hat{k} = \arg\max_{k} \hat{I}(\mathbf{x}, \mathbf{y})$$

MIA is the optimal tool for key recovery when the model is unknown.

Proof sketch

Denoting
$$n_{x,y} = \sum_{i=x,y_i=y}^{m} \mathbb{1}_{x_i=x,y_i=y} = m \hat{\mathbb{P}}(x,y)$$

Empirical Future Work

Experiments showing empirically the optimality of Mutual



 $\hat{\mathbb{P}}(\mathbf{x}|\mathbf{y}) = \prod \hat{\mathbb{P}}(x|y)^{m \,\hat{\mathbb{P}}(x,y)} = 2^{-m\hat{H}(\mathbf{x}|\mathbf{y})}$ $x \in \mathcal{X}, y \in \mathcal{Y}$

where
$$\hat{H}(\mathbf{x}|\mathbf{y}) = \sum_{x \in \mathcal{X}, y \in \mathcal{Y}} \hat{\mathbb{P}}(x, y) \log_2 \frac{1}{\hat{\mathbb{P}}(x|y)}$$
.

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- Information
- Especially, in comparison to Linear Regression Analysis [4]

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