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Design Space Exploration with Deterministic Latency Guarantees for Crossbar MPSoC Architectures

Bogdan Uscumlic*, Andrea Enrici†, Renaud Pacalet†, Amna Gharbi†, Ludovic Apvrille†, Lionel Natarianni* and Laurent Roulet*
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Abstract—MPSoC and NoC systems are often used in complex telecommunication systems, which in the 5G era need to enable telecommunication services with unprecedented latency characteristics. Indeed, new services emerge, needing deterministic latency guarantees with virtually no system jitter, during the lifetime of the established telecommunication service. In this work, for the first time, we propose an optimal solution for a design space exploration (DSE) optimization problem, that performs all the traditional DSE tasks, but with end-to-end deterministic latency guarantees. We focus on MPSoC or NoC architectures with crossbars, although this work can be easily extended to more complex architectures. More precisely, our contributions in this work are the following: 1) we propose a novel method for deterministic scheduling in MPSoC and NoC architectures with a crossbar; 2) we propose an optimal solution in the form of an integer linear program (ILP) for DSE problem with end-to-end deterministic latency guarantees; 3) we identify the trade-off between the latency due to the use of crossbar time slots and the application execution time at different processing elements. The numerical results suggest that the proposed deterministic scheduling method can efficiently use all 100% of the crossbar capacity, depending on available application load and system parameters.

Index Terms—design space exploration, data communication, linear programming, crossbar embedded system architectures.

I. INTRODUCTION

The design space exploration (DSE) problem consists in optimizing the allocation of application tasks to the processing units which are part of an embedded system and in ensuring the allocation of sufficient resources for data communications. This task is very complex, but it becomes even more difficult with the complexity of multi-processor system-on-chip (MPSoC) and network-on-chip (NoC) systems.

Furthermore, recently a new requirement has arisen from the need of Industry 4.0 and 5G systems: the need for deterministic latency. Deterministic or fixed latencies, with strict jitter limitations introduce additional requirements to computer networks, both in optical and electronic domain, but also to NoC and MPSoC systems. The issue of deterministic latency was not really tackled so far in embedded system design space exploration, as it can be seen, e.g. from [1].

Also, new technologies are currently being introduced for facilitating automatic service deployment and orchestration in the 5G context. The cloud-native approach is a novel paradigm for supporting the telecommunication services in 5G architectures. The key idea of this concept is to enable a joint network and cloud infrastructure evolution, with “softwarization” of the telecommunication infrastructure [2]. Cloud-native 5G systems provide many advantages, such as the use of cloud infrastructure for deploying new telecommunication services, reduction of investments, the automation, easy network update, etc. One of the enabling technologies for cloud-native 5G systems is network and computation acceleration, in which FPGAs (Field-Programmable Gate Array) based transport infrastructure play an important role. In such a context, we are interested in looking for the solutions of DSE problems that can benefit from FPGA acceleration and that can model the deterministic latency constraints, as required by 5G applications.

The register allocation and the instruction scheduling are the classical DSE optimization problems in traditional compilers, that can be assessed by using integer linear programming [3]. These problems are NP-hard for realistic processors or NP-complete, when reduced to graph coloring problem [4]. The mapping of applications’ tasks to processing elements in MPSoC and NoC architectures is a DSE problem that can be addressed by using linear programming or constraint programming [5].

However, to the best of our knowledge, an optimal solution of DSE problem with deterministic latency guarantees has not been proposed so far for MPSoC or NoC systems with crossbars. The current work, for the first time, addresses this problem, by using a linear programming approach. We also propose a novel method for crossbar scheduling with deterministic traffic support, in this context.

The remainder of the document is organized as follows. Section II provides more details about the studied hardware platform and the assumptions about the considered DSE problem, with a focus on deterministic latency requirements. Section III is devoted to the related work. In Section IV we describe our mathematical model for the optimal solution of
the above DSE problem based on integer linear programming (ILP) and we detail the proposed crossbar scheduling. In Section V we report the numerical results obtained by using the optimal ILP solution. Finally, the concluding remarks and the perspectives are provided in the final section.

II. CONSIDERED EMBEDDED SYSTEM ARCHITECTURES AND DETERMINISTIC LATENCY GUARANTEES

A. Considered MPSoC and NoC architectures

The typical hardware platform that we consider is heterogeneous and can be composed of different hardware components. These components are different “processing elements” (PE), DMA controllers, memories and various interconnects (e.g. buses, crossbars). The processing elements can be CPUs, GPUs, FPGAs or other components. The use of crossbars is frequent in real-time data flow embedded systems.

This is why in the present work, we focus on modeling a MPSoC or a NoC architecture containing a crossbar. An example of such an architecture is shown in Fig. 1, which illustrates a MPSoC system composed of \( N \) “nodes” (processing elements).

The optimal solution of the DSE problem for the system in Fig. 1 comprises: 1) the allocation of PEs to applications’ tasks; 2) the scheduling of the tasks on the allocated PEs and 3) the crossbar scheduling of data communications between the tasks. Furthermore, in our solution of the DSE problem, the objective function of the optimization minimizes the end-to-end deterministic latency for communications between the tasks. To find such a solution, we model the behavior of the crossbar present in the system.

The applications and their tasks are represented in the form of Homogeneous Synchronous Data Flow (HSDF) graphs, e.g. as shown in Fig. 2. This figure shows the applications considered in the current work, inspired by those studied in [5].

B. Deterministic latency guarantees

Our work, for the first time, takes into account the assumption on the required end-to-end “deterministic” latency guarantees for data communications between the applications’ tasks. Deterministic latency is actually the fixed latency for communications between different points in a MPSoC or NoC system. The guarantees for deterministic latency are usually followed by the requirement for a “zero” jitter. “Zero” jitter usually means that no jitter is present in the system due to the system design or task scheduling. The only present jitter is the one due to the physical effects that cannot be assessed.

After reviewing the related work in the following section, in Section IV we present a mathematical model describing the previously defined DSE problem, together with a method for deterministic scheduling in the crossbars. Please note that our solution with the end-to-end deterministic service guarantees supposes that the traffic benefiting from such a service has a deterministic time profile. In other words, we suppose that the traffic flows exchanged between the applications’ tasks can be represented with the periodic arrivals of equal portions of data. In that way, at the output of the crossbar system, the deterministic traffic profile will be preserved for each flow traversing the system.

III. RELATED WORK

The traditional approach to the mapping of HSDF application graphs to the processing elements consists in decoupling the problem in two steps: assigning actors (computations) to PEs (“spatial allocation” or “mapping”) and ordering the execution of these actors (“temporal allocation” or “scheduling”). However, the complete strategies also exist and they aim at simultaneously retrieving the optimal solution for the mapping and scheduling problems. These complete strategies have the advantage of obtaining more optimized solutions at cost of increased computational complexity. Furthermore, such strategies are attractive for execution scenarios where a solution is computed once and applied during a given time window, when all the relevant characteristics (e.g. dependencies, execution time of functions) are statically known and are guaranteed not to change. These scenarios can be relevant even for modern signal processing (e.g. 5G systems) and multimedia applications. These applications impose, to execution resources, workloads that dynamically evolve over the system’s lifetime.
In this context, historically, the most well-known complete strategy is based on linear programming. Early works are the task partitioning with timing constraints in the SOS system [6], [7] and the mapping in a function of the execution time, processor and communication costs [8]. Furthermore, [9] presents a solution for optimizing the cache memory hierarchy for distributed real-time systems. An alternative approach to linear programming is constraint programming (CP), considered in [5], [10], [11]. While linear programming is more often used to solve the spatial allocation, CP seems to be well suited to solve the temporal allocation [12].

Approximate solutions based on heuristics were also proposed. Very often, the heuristics approximate the optimal solutions described by linear programming models. A comparison of three heuristics based on genetic algorithms, simulated annealing and tabu search is presented in [13]. Other examples are the heuristics considering the scheduling policy [14] or aiming to solve the mapping problem, as in [15] and [16].

More recently, the emergence of complex communication architectures (e.g. crossbars, heterogeneous buses, NoCs) has urged the exploration of novel design spaces. The focus of recent work is more on NoC architectures [17], [18] with the objective of reducing energy consumption, data-access costs and the contention, respectively. The presented work differentiates from the existing work as we target deterministic crossbar based architectures, where our formulation retrieves solutions that guarantee the respect of tight latency constraints that are necessary for deterministic data communications.

IV. INTEGER LINEAR PROGRAMMING SOLUTION FOR THE DSE PROBLEM WITH DETERMINISTIC LATENCY GUARANTEES

The optimal solution of the previously defined problem is formalized by an integer linear programming (ILP) model. The ILP model solves the DSE problem with the end-to-end deterministic latency guarantees (as defined in Section II), for a given MPSoC (or NoC) architecture and for a given set of applications. The list of input parameters to the ILP formulation is given in Tab. I.

The MPSoC architecture is defined by a graph $G(V, E)$ in Tab. I, with graph vertices (nodes) that are enumerated with positive numbers in range $[0, N]$. The links connect the MPSoC nodes with the crossbar (CB), which is supposed to be installed at node “0” of the graph $G(V, E)$. The bandwidth of the links is limited to $BW_l$. The internal bandwidth of the crossbar is limited to $BW_{cb}$.

The notion of “time slots” is introduced to model: 1) the scheduling cycle of all processing elements (equal to $S$ time slots) and 2) the scheduling cycle of the crossbar (equal to $S_{cb}$ time slots). The scheduling of the processing elements and of the crossbar repeats after $S$ and $S_{cb}$ time slots, respectively. The duration of each time slot is expressed in generic “processing time units” [p.t.]. In general case, $S \neq S_{cb}$.

Each application $a$ is represented by a HSDF graph, and it is defined as a set of tasks. Data communication between the tasks $m$ and $n$ of a given application $a$ is described by four different parameters in Tab. I: $T_{m,n,a}$ (for the required link bandwidth); $F_{m,n,a}$, $\alpha_{m,n,a}$ and $\beta_{m,n,a}$ (the crossbar parameters depending on $T_{m,n,a}$). Finally, the worst case processing time of a task $k$ of the application $a$, when running on the PE $i$, is equal to $L_{k,a,i}$.

In Tab. II, we provide a list of the output variables used in the model (all the other variables not listed in Tab. II, but used in the formulation, are binary, auxiliary variables). The key variables are $x_{l,k,a}^i$ and $s_{l,k,a}^i$, which determine which PE is allocated to which application and the processing starting times at different PEs, respectively.

Next, Tab. III provides the formulation constraints. In this table and in the remainder of this paper, the following index notation is used: $i, j \in V /\{0\}$, $a \in A$, $\sigma \in [0, S_{cb} - 1]$ and $l \in E$ (the sets and the values $V$, $A$, $S_{cb}$ and $E$ are defined in Tab. I). Please note that the solution provided by a ILP formulation is optimal, for a specified objective function. In our case, the objective function (eq. (1) in Tab. III) minimizes the total end-to-end deterministic latency for each pair of tasks that communicate directly (as defined by the HSDF graph of the application containing these tasks). In the following, we discuss in detail all the constraints from Tab. III.


### Table II: Output Variables

<table>
<thead>
<tr>
<th>Output Variables</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x_{i,j}^{k,a}$</td>
<td>Binary = 1 if the task $(k,a)$ is allocated at PE $i$, otherwise.</td>
</tr>
<tr>
<td>$z_{i,j}^{m,n,a}$</td>
<td>Binary = 1 if the tasks $m$ and $n$ are allocated at PEs $i$ and $j$, respectively, or 0, otherwise.</td>
</tr>
<tr>
<td>$s_{i,j}^{k,a}$</td>
<td>Natural, indicating the starting time slot (in the range $[1,S]$) for the execution of the task $(k,a)$ at PE $i$, equal to 0 if $k$ is not installed at PE $i$.</td>
</tr>
<tr>
<td>$m_{i,j}$</td>
<td>Binary = 1 if the matching between input/output ports $i$ and $j$ of the crossbar happens at time slot $\sigma$, or 0, otherwise.</td>
</tr>
<tr>
<td>$B_{i,j}^{m,n,a}$ / $B_{i,j}^{m,n,a,\sigma}$</td>
<td>Binaries, = 1 if the $(m,n,a)$ traffic in the crossbar, exchanged between PEs $i$ and $j$, is transported starting from/by using (respectively) the time slot $\sigma$ or 0, otherwise.</td>
</tr>
</tbody>
</table>

### Table III: Integer Linear Programming Formulation

<table>
<thead>
<tr>
<th>No.</th>
<th>Constraint</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1)</td>
<td>$\sum_{m,n,a} \sum_{(i,j)\in T_{m,n,a}} (L_{i,j} + \sum_{l=1}^{\sigma} M_{i,j,l}) \leq \sum_{(i,j)\in T_{m,n,a}} z_{i,j}^{k,a}$</td>
</tr>
<tr>
<td>(2)</td>
<td>$\sum_{n,a} \sum_{(i,j)\in T_{m,n,a}} z_{i,j}^{k,a} \leq x_{i,j}^{k,a}$</td>
</tr>
<tr>
<td>(3)</td>
<td>$\sum_{m,n,a} \sum_{(i,j)\in T_{m,n,a}} x_{i,j}^{k,a} \leq n_{i,j}^{k,a}$</td>
</tr>
<tr>
<td>(4)</td>
<td>$\sum_{i,j} z_{i,j}^{k,a} \geq 1, \forall (m,n) \in a^2, \forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(5)</td>
<td>$\sum_{i,j} z_{i,j}^{k,a} \leq 1, \forall a, \forall \sigma$</td>
</tr>
<tr>
<td>(6)</td>
<td>$\sum_{i,j} (1-x_{i,j}^{k,a}) \leq \sum_{i,j} (1-z_{i,j}^{k,a})$, $\forall (m,n,a) \in a^2$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(7)</td>
<td>$s_{i,j}^{k,a} \leq x_{i,j}^{k,a}$, $\forall i,j \in a$, $\forall k,a \in a$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(8)</td>
<td>$s_{i,j}^{k,a} + L_{k,a} \leq S + 1, \forall i,j \in a$, $\forall k,a \in a$</td>
</tr>
<tr>
<td>(9)</td>
<td>$s_{i,j}^{k,a} + L_{k,a} \leq S + 1, \forall i,j \in a$, $\forall k,a \in a$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(10)</td>
<td>$s_{i,j}^{k,a} + L_{k,a} \leq S + 1, \forall i,j \in a$, $\forall k,a \in a$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(11)</td>
<td>$s_{i,j}^{k,a} + L_{k,a} \leq S + 1, \forall i,j \in a$, $\forall k,a \in a$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(12)</td>
<td>$\sum_{(i,j)\in T_{m,n,a}} (M_{i,j} + \sum_{l=1}^{\sigma} M_{i,j,l}) \leq \sum_{(i,j)\in T_{m,n,a}} z_{i,j}^{k,a} \leq 1, \forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(13)</td>
<td>$\sum_{(i,j)\in T_{m,n,a}} (M_{i,j} + \sum_{l=1}^{\sigma} M_{i,j,l}) \leq \sum_{(i,j)\in T_{m,n,a}} z_{i,j}^{k,a} \leq 1, \forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(14)</td>
<td>$\sum_{(i,j)\in T_{m,n,a}} (M_{i,j} + \sum_{l=1}^{\sigma} M_{i,j,l}) \leq \sum_{(i,j)\in T_{m,n,a}} z_{i,j}^{k,a} \leq 1, \forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(15)</td>
<td>$B_{i,j}^{m,n,a} = B_{i,j}^{m,n,a,\sigma}$, $\forall (m,n) \in a^2$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
<tr>
<td>(16)</td>
<td>$0 \leq \sum_{(i,j)\in T_{m,n,a}} B_{i,j}^{m,n,a,\sigma} \leq n_{i,j}^{k,a}$, $\forall \sigma \in T_{m,n,a}$</td>
</tr>
</tbody>
</table>

### A. Constraints ensuring the allocation of PEs

The constraint (2) ensures that tasks and applications can be allocated only at the allowed subsets of PEs (these subsets are defined by the input parameters $T_{k,a,i}$). The constraint holds for each task that is an origin (i.e., a “source”) of data communication towards some other task in a HSDF graph. The constraint (3) has the same role as the previous constraint, but it holds for the tasks receiving some traffic from other tasks in HSDF graphs.

Next, for a given pair of tasks $(m,n)$ that are directly connected in the HSDF graph of an application $a$ (resulting in $T_{m,n,a} \neq 0$), there must exist only a single pair of processing elements $i$, $j$ (on the MPSoC chip), to which the tasks $m$ and $n$ are allocated, respectively. This property is ensured by the constraint (4).

The constraint (5) ensures that at most one PE can be allocated to a given task and a given application. Finally, to limit the capacity of data communications over each link in MPSoC, we use the constraint (6).

So far, the constraints were dealing with properly allocating PEs to applications’ tasks. These constraints provide the basic limitations on the PE allocation variables: $x_{i,j}^{k,a}$ and $z_{i,j}^{k,a}$. Next, we address the scheduling of tasks on PEs.

### B. Constraints for the scheduling of tasks on PEs

The key variable defining the scheduling of tasks on PEs in MPSoC is $s_{i,j}^{k,a}$. This variable defines the starting time of execution of the task $(k,a)$ at PE $i$. To simplify the constraints, the possible values of $s_{i,j}^{k,a}$ are situated in the range $[1,S]$.

The function of the following constraint, (7), is to connect the variables $x_{i,j}^{k,a}$ and $s_{i,j}^{k,a}$. Indeed, $x_{i,j}^{k,a}$ and $s_{i,j}^{k,a}$ can both be different than 0, but only simultaneously. The constraint (8), provided next, make sure that the total execution time of each task at a given PE is not greater than the end of the scheduling period $S$.

The constraints also need to address the case when tasks of different applications share the same PE. This is achieved by the constraint (9). For proper functioning of the constraint, the following two conditions need to be satisfied: 1) the inequality connecting the variables $s_{i,j}^{k,a}$ needs to take into account the order of their scheduling on the PE (this is achieved by introducing the auxiliary decision variable $\delta_{i,j}^{k,a}$), and 2) the condition can be enforced only if the allocation of PEs to applications’ tasks also holds (this is achieved by introducing the auxiliary decision variable $\delta_{i,j}^{k,a}$).

Next, when scheduling two tasks of the same application on the same PE, if the tasks “directly communicate”, the task that is the origin of direct communication shall be executed first, which is enabled by the constraint (10). Similarly, the inequality (11) is needed to set the scheduling relation between different tasks of a given application.
variables \( B \) are the scheduling constraints, calculating the key scheduling deterministic data communications. The constraints (14)-(16) and (13) limits the total available capacity for transport of traffic flow is equal to \( \alpha \) (i.e. they define \( \alpha_{m,n,a} \) and \( \beta_{m,n,a} \)).

C. Model and constraints for the crossbar scheduling

The architecture of the crossbar is shown in Fig. 3. We suppose that the crossbar operates in discrete time slots. The scheduling in the crossbar repeats after the scheduling cycle of \( S_{cb} \) time slots. Each time slot is allocated to one pair of input-output links. The bandwidth available during the input-output interconnection traversing the crossbar is equal to \( BW_{cb} \). Time slot allocation is always performed in a way that satisfies the matching condition of the crossbar. “Matching” is a crossbar configuration property according to which no more than a single output can be connected to any single input (and vice versa), at any given time.

Data communications are supposed to be periodic (deterministic), as in Fig. 3. The scheduling in the crossbar allows to multiplex different applications’ tasks at each PE connected to the crossbar. When multiplexing data, the size of “flow periods” of different data flows must correspond to the value of \( S_{cb} \). Indeed, the “flow period” (defined in Tab. I) for \((m,n,a)\) traffic flow is equal to \( \alpha_{m,n,a} + \beta_{m,n,a} \). This is why, in order to ensure a feasible solution for the crossbar scheduling, we suppose that \( S_{cb} \) is equal to the least common multiple of all flow periods \( \alpha_{m1,n1,a1} + \beta_{m1,n1,a1}, \alpha_{m2,n2,a2} + \beta_{m2,n2,a2}, \ldots, \)

In the formulation, the constraint (12) is introduced to enforce the matching condition in the crossbar. The capacity constraint (13) limits the total available capacity for transport of deterministic data communications. The constraints (14)-(16) are the scheduling constraints, calculating the key scheduling variables \( B_{i,j}^{m,n,a} \) and \( p_{i,j}^{m,n,a} \). Finally, to connect different variables describing the crossbar and the PE allocation process, we introduce the constraints (17) and (18).

Please note that the previously defined DSE problem becomes equivalent to traditional processor allocation problem for \( N = 3 \). The latter problem is generally considered to be NP-hard for the objective functions that optimize applications’ performances [1], so it can be considered that our DSE problem has the same computational complexity.

1“Direct communication” relates to the presence of a connecting arrow in HSDF graph.

Fig. 3. Crossbar architecture with the periodic scheduling model (with scheduling period \( S_{cb} \)). \( \alpha(i) \) and \( \beta(i) \) correspond to \( "(m_i,n_i,a_i) \) traffic”, i.e. they define \( \alpha_{m_i,n_i,a_i} \) and \( \beta_{m_i,n_i,a_i} \).

V. Numerical results

We have implemented the previous ILP formulation in the IBM CPLEX software. In this section we report the optimal results of simulations, for various application assumptions.

A. The application assumptions

We consider a motivating example and three application scenarios. In the following, we describe the application assumptions for the scenarios 1, 2 and 3, while the motivating example has slightly different assumptions. All the values chosen here are for illustration purpose, and can be changed for different set of applications and PEs. We suppose that \( \Gamma_{k,a,i} = 1 \) (\( \forall k, \forall a, \forall i \)) and \( L_{cb}(i,j) = 2 \) p.t. (\( \forall i, \forall j \)), which corresponds to the latency of CB. Next, \( N = 4, S_{cb} = 8 \) p.t., \( BW_{i} = 1.2 \) Gbit/s and \( BW_{cb} = 133 \) Mbit/s.

The capacity \( v_{m,n,a} \) of each \((m,n,a)\) traffic flow is written next to the corresponding link in Fig. 2. In this figure, value of \( v_{m,n,a} \) is given in (crossbar) time slots. The link bandwidth required for the \((m,n,a)\) traffic flow is then equal to \( T_{m,n,a} = v_{m,n,a}/S_{cb} \cdot BW_{cb} \). Other assumptions on the considered applications (from Fig. 2) are summarized in Tab. IV. We consider the following three application scenarios:

1) Scenario 1. Linear combination of applications A and B. We consider that \( S = 10 \). The application load increases and the results are calculated for the points \{B, A+B, A+2B, 2A+2B, ...\} This scenario illustrates the achievable crossbar time slot occupancy (i.e. the average percentage of occupied crossbar time slots over the active input-output connections).

2) Scenario 2. Fixed application load of 2A+2B. For such fixed application load, we increase the value of \( S \), starting from \( S = 10 \) (we increase the computational power of PEs), to study the dependency of the optimal solution and the crossbar time slot occupancy from the available processing power in the system.

3) Scenario 3. Randomly chosen application load from the set \{A, B, C, D, E\}. For \( S = 17 \), the application load is randomly generated out of the applications from Fig. 2. This scenario illustrates the behavior of the scheduling and the PE allocation process in case of random application load.

B. Motivating example: 3-node crossbar architecture

First, for illustration purposes, we consider a simple crossbar system composed of three nodes (\( N = 2 \)), as in Fig. 4. The applications to be allocated in this system are the applications A and B from Fig. 2, with the same assumptions as in Tab. IV. The size of scheduling cycle on any PE is supposed to be \( S = 5 \) p.t., while \( S_{cb} \) and all the other parameters have the same values as in Scenarios 1, 2 and 3.
TABLE IV
APPLICATIONS IN FIG. 2

<table>
<thead>
<tr>
<th>Application:</th>
<th>Assumptions (all values are in “time slots” or [p.t.]; CB is installed at the node defined by i = 0):</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>$L_{A1,A1} = 1$, (tri) $i = 1$, $L_{A1,A1,i} = L_{A1,A1,i+1}$, $L_{A2,A1} = 4$, (tri) $i = 1$, $L_{A2,A1,i} = L_{A2,A1,i+1}$, $L_{A3,A2} = 2$, (tri) $i = 4$, $L_{A3,A2,i} = L_{A3,A2,i+1}$, $L_{A4,A3} = 2$, (tri) $i = 4$, $L_{A4,A3,i} = L_{A4,A3,i+1}$, $L_{A5,A4} = 2$, (tri) $i = 4$, $L_{A5,A4,i} = L_{A5,A4,i+1}$</td>
</tr>
<tr>
<td>B</td>
<td>$L_{B1,B1} = 2$, (tri) $i = 4$, $L_{B1,B1,i} = L_{B1,B1,i+1}$, $L_{B1,B1,B1} = 1$, (tri) $i = 4$, $L_{B1,B1,B1,i} = L_{B1,B1,B1,i+1}$, $L_{B2,B2} = 1$, (tri) $i = 4$, $L_{B2,B2,i} = L_{B2,B2,i+1}$, $L_{B3,B3} = 2$, (tri) $i = 4$, $L_{B3,B3,i} = L_{B3,B3,i+1}$</td>
</tr>
<tr>
<td>C</td>
<td>$L_{C1,C1} = 2$, (tri) $i = 1$, $L_{C1,C1,i} = L_{C1,C1,i+1}$, $L_{C2,C2} = 1$, (tri) $i = 2$, $L_{C2,C2,i} = L_{C2,C2,i+1}$, $L_{C3,C3} = 1$, (tri) $i = 2$, $L_{C3,C3,i} = L_{C3,C3,i+1}$, $L_{C4,C4} = 1$, (tri) $i = 2$, $L_{C4,C4,i} = L_{C4,C4,i+1}$, $L_{C5,C5} = 1$, (tri) $i = 2$, $L_{C5,C5,i} = L_{C5,C5,i+1}$</td>
</tr>
<tr>
<td>D</td>
<td>$L_{D1,D1} = 1$, (tri) $i = 6$, $L_{D1,D1,i} = L_{D1,D1,i+1}$, $L_{D2,D2} = 1$, (tri) $i = 6$, $L_{D2,D2,i} = L_{D2,D2,i+1}$, $L_{D3,D3} = 4$, (tri) $i = 6$, $L_{D3,D3,i} = L_{D3,D3,i+1}$, $L_{D4,D4} = 1$, (tri) $i = 6$, $L_{D4,D4,i} = L_{D4,D4,i+1}$</td>
</tr>
<tr>
<td>E</td>
<td>$L_{E1,E1} = 2$, (tri) $i = 1$, $L_{E1,E1,i} = L_{E1,E1,i+1}$, $L_{E2,E2} = 1$, (tri) $i = 1$, $L_{E2,E2,i} = L_{E2,E2,i+1}$, $L_{E3,E3} = 3$, (tri) $i = 3$, $L_{E3,E3,i} = L_{E3,E3,i+1}$, $L_{E4,E4} = 1$, (tri) $i = 1$, $L_{E4,E4,i} = L_{E4,E4,i+1}$, $L_{E5,E5} = 4$, (tri) $i = 1$, $L_{E5,E5,i} = L_{E5,E5,i+1}$, $L_{E6,E6} = 2$, (tri) $i = 1$, $L_{E6,E6,i} = L_{E6,E6,i+1}$, $L_{E7,E7} = 1$, (tri) $i = 1$, $L_{E7,E7,i} = L_{E7,E7,i+1}$</td>
</tr>
</tbody>
</table>

The resulting scheduling on PEs in the motivating example is shown in Fig. 5. The value of the objective function (the end-to-end deterministic latency) is equal to 13 p.t. (indeed, the overall latencies for traffic flows (A1, A2), (A1, A3, A) and (B1, B2) are 5, 5 and 3 p.t., respectively). The traffic flow (A1, A3, A) is routed over the crossbar. The results show that the crossbar latency between the tasks A1 and A3 has been properly taken into account.

C. Results for a crossbar architecture with $N = 4$

Next, Scenarios 1, 2 and 3 are considered in a larger MPSoC, composed of five nodes (i.e. for $N = 4$ in Fig. 1).

1) Scenario 1: The simulation results are provided in Fig. 6, for linearly increasing application load. The figure shows the increase of the objective function value (the end-to-end deterministic latency) with the increase of the scheduled load. One of the key results is that the crossbar slots can be highly...

![Fig. 5](image-url)  The resulting scheduling on PEs in the motivating example

![Fig. 6](image-url)  Scenario 1: total end-to-end deterministic latency and CB slot occupancy for a linearly increasing traffic load

![Fig. 7](image-url)  Scenario 2: total end-to-end deterministic latency and CB slot occupancy for a fixed traffic load

![Fig. 8](image-url)  Scenario 3: total end-to-end deterministic latency and CB slot occupancy for a random traffic load
occupied (up to 100%), for sufficiently high data communication loads. This confirms the efficiency of the proposed deterministic scheduling method for the slot allocation in the crossbar. These results also identify a trade-off between the use of crossbar’s time slots (which introduces the crossbar transit latency) and the use of processing elements’ time slots.

2) Scenario 2: In order to further explore the trade-off between the use of the crossbar and PEs in MPSoC architecture, we test Scenario 2 in the same five-node MPSoC topology. The simulation results are provided in Fig. 7. We observe what happens with the increase of the computational power of PEs. We mimick the computational power increase with the increase of the scheduling cycle $S$ for a fixed application load (indeed, without changing the values of tasks’ processing times $L_{k,n,i}$, the increase of $S$ is equivalent to the increase of PE’s computational capacity).

Fig. 7 clearly shows that the increase of computational power of processing elements results in:

- the decrease of the objective function value; indeed, the increase of the computational power of PEs allows to tasks to use “cheaper” processing elements, i.e. those that are more efficient in terms of latency.
- the decrease of the crossbar time slot occupancy; indeed, this is another expected outcome, since the use of crossbar is penalized by the crossbar latency (supposed to be 2 p.t. in this example), so the crossbar will be used only when needed.

3) Scenario 3: Finally, in Scenario 3, we increase the total application load in the system. Furthermore, the applications are randomly generated, to test the behavior of the scheduling and the PE allocation process for a randomly generated application matrix.

The results are summarized in Fig. 8. The found values of the end-to-end deterministic latency are higher in this case, because the maximum application load is greater than in the previous scenarios. The time slots in the crossbar are used up to 37.5 %, with tendency of increased time slot use at higher loads. Indeed, for lower application loads, there are still available time slots at latency-efficient PEs, so the use of crossbar is not required. This trend does not differ in linear and random load scenario. Furthermore, such behavior once again confirms the trade-off between the use of time slots in the crossbar and at processing elements.

VI. CONCLUSIONS AND PERSPECTIVES

We have proposed an optimal solution for the DSE problem in a crossbar MPSoC system. Our solution and scheduling model for the first time provide end-to-end deterministic latency guarantees in such a context. The optimal solution of DSE problem is based on an integer linear program. The new optimization problem has a high computational complexity.

We have identified a trade-off between the use of crossbar’s time slots for supporting data communications and the use of processing elements’ time slots. Since the crossbar introduces latency, the optimal solution will use the crossbar time slots as needed, and in a proportion corresponding to the relative “cost” of crossbar communication latency and processing latency at different processing elements.

By using the proposed optimal solution as a benchmark, an approximate heuristic algorithm can be developed, that would be able to solve large instances of the problem, in a minimum computation time. The development of such a solution is left for future work. Such approximate algorithm could be then used in the context of accelerated processing with deterministic latency guarantees in cloud-native 5G systems.

REFERENCES