

Maximizing the success of a side-channel attack

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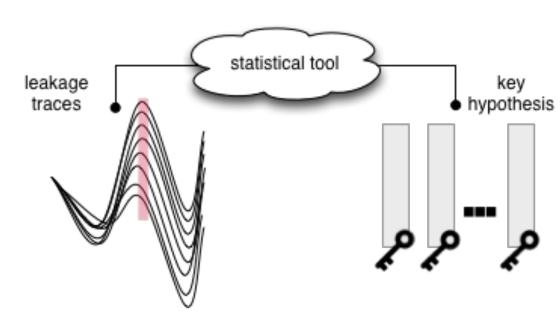
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State of the Art

- ♦ What distinguishes known distinguishers, in terms of distinctive features?
- ♦ Given a side-channel context, what is the best distinguisher amongst all known ones?
- Distinguishers were chosen as (arbitrary) **statistical tools** (correlation, difference of means, linear regression, etc.)
- [1] highlights that proposed distinguishers behave **equivalent** when using the same leakage model, only "statistical artifacts" can explain different behavior [2]
- The **estimation** of the statistical tools (esp. mutual information) is very crucial and effective on the success [3]



- [1] Doget, Prouff, Rivain, and Standaert, JCEN, 2011
- [2] Mangard, Oswald, and Standaert. IET, 2011
- [3] Prouff and Rivain, IJACT, 2010.
- [4] Heuser, Rioul, and Guilley, under submission

Side-channel analysis as a communication problem [4]

- ♦ Given a side-channel scenario, what is the best distinguisher, amongst all possible ones?
- Idea: Translate the problem of side-channel analysis into a problem of communication theory → derive optimal distinguisher: maximize the success rate
- Leakage model is known to the attacker (**Theorem 1**)
 - Only statistical noise
 - Optimal decoding rule $\arg\max_k \Big(\mathbb{P}\{k\} \cdot p(\mathbf{x}|\mathbf{y}(k)) \Big)$ (template attack, profiling is possible)
 - The optimal distinguisher only depends on the noise distribution (e.g., Laplacian, uniform, Gaussian)
- Leakage model is partially unknown to the attacker (**Theorem 2**)
 - Statistical and epistemic noise
 - Leakage arises due to a weighted sum of bits, where the weights follow a normal distribution

side-channel notations leakage leakage variable function distinguisher guess $\mathbf{Y}(k^*)$ source channel decoded channel decoder encoder message output digital communication notations

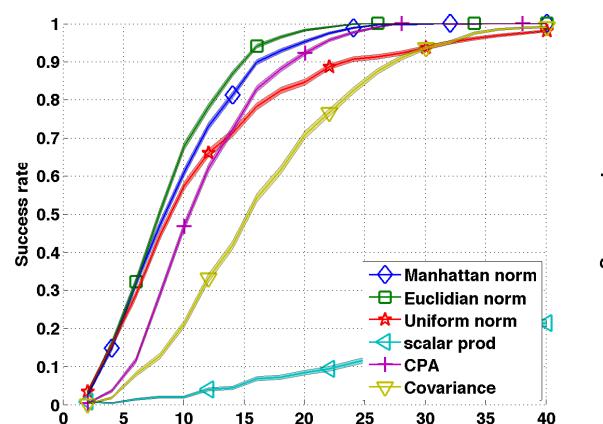
Theorem 2: optimal distinguisher when the leakage model is partially unknown

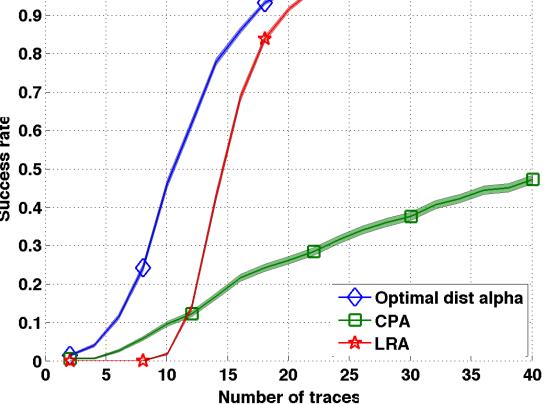
Let
$$\mathbf{Y}_{\alpha}(k) = \sum_{j=1}^n \alpha_j [f(\mathbf{T},k)]_j$$
, $\mathbf{Y}_j(k) = [f(\mathbf{T},k)]_j$ and $\mathbf{X} = \sum_{j=1}^n \alpha_j [f(T,k^\star)]_j + N$

with $N \sim \mathcal{N}(0, \sigma^2)$. Assuming weights are independently deviating normally from the Hamming weight model, then the optimal distinguishing rule is

$$\mathcal{D}^{\alpha,G}(\mathbf{x},\mathbf{t}) = \arg\max_{k} \left(\gamma \langle \mathbf{x} | \mathbf{y}(k) \rangle + \mathbf{1} \right)^{t} \cdot (\gamma Z(k) + I)^{-1} \cdot (\gamma \langle \mathbf{x} | \mathbf{y}(k) \rangle + \mathbf{1})$$
$$-\sigma_{\alpha}^{2} \ln \det(\gamma Z(k) + I) ,$$

where $\gamma = \frac{\sigma_{\alpha}^2}{\sigma^2}$ is the epistemic-to-stochastic-noise-ratio (ESNR).





Known model

Number of traces

Partially unknown model

Theorem 1: optimal distinguisher when the leakage model is known

If the leakage arises from $X=Y(k^\star)+N$ with known leakage model $Y(k)=\varphi(f(k,T))$ then the optimal distinguishing rule are

- Gaussian noise distribution: $\mathcal{D}_{opt}^{M,G}(\mathbf{x},\mathbf{t}) = \arg\max_k \langle \mathbf{x} | \mathbf{y}(k) \rangle \frac{1}{2} ||\mathbf{y}(k)||_2^2$,
- Uniform noise distribution: $\mathcal{D}_{opt}^{M,U}(\mathbf{x},\mathbf{t}) = \arg\max_{k} \|\mathbf{x} \mathbf{y}(k)\|_{\infty}$,
- Laplace noise distribution: $\mathcal{D}_{opt}^{M,L}(\mathbf{x},\mathbf{t}) = \arg\max_{k} \|\mathbf{x} \mathbf{y}(k)\|_{1}$.

Correlation
Covariance
Linear regression

Our novel **optimal** distinguishers **outperform** all state-of-the-art
distinguishers depending on statistical
tools in terms of the **success rate**!